

Adding and Subtracting Radical Expressions

Simplify.

1) $3\sqrt{6} - 4\sqrt{6} = -\sqrt{6}$

2) $-3\sqrt{7} + 4\sqrt{7} = \sqrt{7}$

3) $-11\sqrt{21} - 11\sqrt{21} = -22\sqrt{21}$

4) $-9\sqrt{15} + 10\sqrt{15} = \sqrt{15}$

5) $-10\sqrt{7} + 12\sqrt{7} = 2\sqrt{7}$

6) $-3\sqrt{17} - 4\sqrt{17} = -7\sqrt{17}$

7) $-10\sqrt{11} - 11\sqrt{11} = -21\sqrt{11}$

8) $-2\sqrt{3} + 3\sqrt{27}$
 $= -2\sqrt{3} + 3\sqrt{9 \cdot 3}$
 $= -2\sqrt{3} + 3 \cdot 3\sqrt{3}$
 $= -2\sqrt{3} + 9\sqrt{3}$
 $= 7\sqrt{3}$

9) $2\sqrt{6} - 2\sqrt{24}$
 $= 2\sqrt{6} - 2\sqrt{4 \cdot 6}$
 $= 2\sqrt{6} - 4\sqrt{6}$
 $= -2\sqrt{6}$

10) $2\sqrt{6} + 3\sqrt{54}$
 $2\sqrt{6} + 3\sqrt{9 \cdot 6} = 2\sqrt{6} + 3 \cdot 3\sqrt{6}$
 $= 2\sqrt{6} + 9\sqrt{6}$
 $= 11\sqrt{6}$

11) $-\sqrt{12} + 3\sqrt{3}$
 $= -\sqrt{4 \cdot 3} + 3\sqrt{3}$
 $= -2\sqrt{3} + 3\sqrt{3}$
 $= \sqrt{3}$

12) $3\sqrt{3} - \sqrt{27}$
 $3\sqrt{3} - \sqrt{9 \cdot 3} = 3\sqrt{3} - 3\sqrt{3} = 0$

$$\begin{aligned}
 13) \quad 3\sqrt{8} + 3\sqrt{2} &= 3\sqrt{4 \cdot 2} + 3\sqrt{2} \\
 &= 3 \cdot 2\sqrt{2} + 3\sqrt{2} \\
 &= 6\sqrt{2} + 3\sqrt{2} \\
 &= 9\sqrt{2}
 \end{aligned}$$

$$\begin{aligned}
 15) \quad -3\sqrt{20} - \sqrt{5} &= -3\sqrt{4 \cdot 5} - \sqrt{5} \\
 &= -3 \cdot 2\sqrt{5} - \sqrt{5} \\
 &= -6\sqrt{5} - \sqrt{5} \\
 &= -7\sqrt{5}
 \end{aligned}$$

$$\begin{aligned}
 17) \quad 3\sqrt{18} - 2\sqrt{2} &= 3\sqrt{9 \cdot 2} - 2\sqrt{2} \\
 &= 3 \cdot 3\sqrt{2} - 2\sqrt{2} \\
 &= 9\sqrt{2} - 2\sqrt{2} \\
 &= 7\sqrt{2}
 \end{aligned}$$

$$\begin{aligned}
 19) \quad 3\sqrt{18} + 3\sqrt{12} + 2\sqrt{27} \\
 3\sqrt{9 \cdot 2} + 3\sqrt{4 \cdot 3} + 2\sqrt{9 \cdot 3} \\
 9\sqrt{2} + 6\sqrt{3} + 6\sqrt{3} \\
 9\sqrt{2} + 12\sqrt{3}
 \end{aligned}$$

$$\begin{aligned}
 21) \quad -3\sqrt{2} + 3\sqrt{20} - 3\sqrt{8} \\
 -3\sqrt{2} + 3\sqrt{4 \cdot 5} - 3\sqrt{4 \cdot 2} \\
 -3\sqrt{2} + 6\sqrt{5} - 6\sqrt{2} \\
 6\sqrt{5} - 9\sqrt{2}
 \end{aligned}$$

$$\begin{aligned}
 23) \quad -2\sqrt{20} + 2\sqrt{18} - 2\sqrt{5} \\
 -2\sqrt{4 \cdot 5} + 2\sqrt{9 \cdot 2} - 2\sqrt{5} \\
 -4\sqrt{5} + 6\sqrt{2} - 2\sqrt{5} \\
 6\sqrt{2} - 6\sqrt{5}
 \end{aligned}$$

$$\begin{aligned}
 25) \quad -\sqrt{45} + 2\sqrt{5} - \sqrt{20} - 2\sqrt{6} \\
 -\sqrt{9 \cdot 5} + 2\sqrt{5} - \sqrt{4 \cdot 5} - 2\sqrt{6} \\
 -3\sqrt{5} + 2\sqrt{5} - 2\sqrt{5} - 2\sqrt{6} \\
 -3\sqrt{5} - 2\sqrt{6}
 \end{aligned}$$

$$\begin{aligned}
 27) \quad -3\sqrt{45} + 2\sqrt{12} + 3\sqrt{6} - 3\sqrt{20} \\
 -3\sqrt{9 \cdot 5} + 2\sqrt{4 \cdot 3} + 3\sqrt{6} - 3\sqrt{4 \cdot 5} \\
 -9\sqrt{5} + 4\sqrt{3} + 3\sqrt{6} - 6\sqrt{5} \\
 -15\sqrt{5} + 4\sqrt{3} + 3\sqrt{6}
 \end{aligned}$$

$$14) \quad -3\sqrt{6} + 3\sqrt{6} = 0$$

$$\begin{aligned}
 16) \quad 2\sqrt{45} - 2\sqrt{5} &= 2\sqrt{9 \cdot 5} - 2\sqrt{5} \\
 &= 6\sqrt{5} - 2\sqrt{5} \\
 &= 4\sqrt{5}
 \end{aligned}$$

$$\begin{aligned}
 18) \quad -3\sqrt{18} + 3\sqrt{8} - \sqrt{24} &= -3\sqrt{9 \cdot 2} + 3\sqrt{4 \cdot 2} - \sqrt{4 \cdot 6} \\
 &= -9\sqrt{2} + 6\sqrt{2} - 2\sqrt{6} \\
 &= -3\sqrt{2} - 2\sqrt{6}
 \end{aligned}$$

$$20) \quad -3\sqrt{5} - \sqrt{6} - \sqrt{5} = -4\sqrt{5} - \sqrt{6}$$

$$\begin{aligned}
 22) \quad -3\sqrt{3} - \sqrt{8} - 3\sqrt{3} &= -6\sqrt{3} - \sqrt{4 \cdot 2} \\
 &= -6\sqrt{3} - 2\sqrt{2}
 \end{aligned}$$

$$\begin{aligned}
 24) \quad 2\sqrt{18} - 2\sqrt{12} + 2\sqrt{18} &= 2\sqrt{9 \cdot 2} - 2\sqrt{4 \cdot 3} + 2\sqrt{9 \cdot 2} \\
 &= 6\sqrt{2} - 4\sqrt{3} + 6\sqrt{2} \\
 &= 12\sqrt{2} - 4\sqrt{3}
 \end{aligned}$$

$$\begin{aligned}
 26) \quad 2\sqrt{20} - \sqrt{20} + 3\sqrt{20} - 2\sqrt{45} \\
 2\sqrt{4 \cdot 5} - \sqrt{4 \cdot 5} + 3\sqrt{4 \cdot 5} - 2\sqrt{9 \cdot 5} \\
 4\sqrt{5} - 2\sqrt{5} + 6\sqrt{5} - 6\sqrt{5} \\
 2\sqrt{5}
 \end{aligned}$$

$$\begin{aligned}
 28) \quad -\sqrt{27} - 3\sqrt{45} - \sqrt{20} + 2\sqrt{45} \\
 -\sqrt{9 \cdot 3} - 3\sqrt{9 \cdot 5} - \sqrt{4 \cdot 5} + 2\sqrt{9 \cdot 5} \\
 -3\sqrt{3} - 9\sqrt{5} - 2\sqrt{5} + 6\sqrt{5} \\
 -3\sqrt{3} - 5\sqrt{5}
 \end{aligned}$$